

Math 115

Spring 2017

Lecture 7

John paid \$12 to purchase 20 items at some sale. At this rate, how much does he have to pay for 75 items?

$$\frac{\$12}{20 \text{ items}} = \frac{\$x}{75 \text{ items}} \quad \text{Solve } \frac{12}{20} = \frac{x}{75}$$

Cross-Multiply

$$20x = 12(75)$$

$$x = \frac{12(75)}{20}$$

$$\Rightarrow \boxed{x = 45}$$

He needs \$45 to pay for 75 items.

7.5% of what number is 2250?

① By translation:

$$\frac{7.5}{100} \cdot x = 2250$$

$$.075 x = 2250$$

$$x = \frac{2250}{.075}$$

$$x = 30,000$$

7.5% of 30,000 is 2250.

② By Proportion

$$\frac{7.5}{100} = \frac{2250}{x}$$

$$\frac{P}{100} = \frac{\text{Part}}{\text{whole}}$$

"Part comes after is"
"whole comes after of"

$$\frac{7.5}{100} = \frac{2250}{x}$$

cross-multiply

$$7.5x = 100(2250)$$

$$x = \frac{100(2250)}{7.5}$$

$$x = 30,000$$

7.5% of 30,000 is 2250.

what percent of 12500 is 500?

$$\frac{P}{100} \cdot 12500 = 500$$

$$125P = 500$$

$$P = 4$$

4%

$$\frac{P}{100} = \frac{\text{Part}}{\text{whole}}$$

$$\frac{P}{100} = \frac{500}{12500}$$

$$12500P = 50000$$

$$P = 4$$

4%

A TV is on Sale at 15% off.

The original price was \$750.

Find the amount of discount.

Find the Sales amount.

Amount of discount is 15% of original Price

Amount of Sale price is 85% of - - - -

$$\text{Discount} = \frac{15}{100} \cdot 750 \Rightarrow \text{Discount} = \$112.50$$

$$\text{Sale Price} = \frac{85}{100} \cdot 750 \Rightarrow \text{Sale Price} = \frac{\$637.50}{\text{Original} = \$750}$$

Solve:

$$-4(x-1) + 10 \leq x - 26$$

$$-4x + 4 + 10 \leq x - 26$$

$$-4x + 14 \leq x - 26$$

$$-4x - x \leq -26 - 14$$

$$-5x \leq -40$$

$$\frac{-5}{-5}x \geq \frac{-40}{-5}$$

$$x \geq 8$$

S.B.N.

$$\{x \mid x \geq 8\}$$

Graph



I.N.

$$[8, \infty)$$

Solve

$$\frac{1}{3}x - \frac{3}{4} > \frac{5}{6}x + \frac{2}{3}$$

Use LCD = 12, to clear fractions.

$$\cancel{12} \cdot \frac{1}{\cancel{3}}x - \cancel{12} \cdot \frac{3}{\cancel{4}} > \cancel{12} \cdot \frac{5}{\cancel{6}}x + \cancel{12} \cdot \frac{2}{\cancel{3}}$$

$$4x - 9 > 10x + 8$$

$$4x - 10x > 8 + 9$$

$$-6x \boxed{>} 17$$

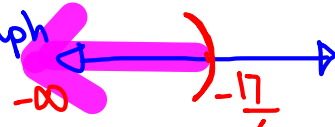
$$\frac{-6}{-6}x < \frac{17}{-6}$$

$$x < -\frac{17}{6}$$

① S.B.N.

$$\{x \mid x < -\frac{17}{6}\}$$

② Graph



③ I.N.

$$(-\infty, -\frac{17}{6})$$

Solve $-2 < 3x + 7 \leq 19$ Hint: Isolate x in the middle

$$-2 - 7 < 3x \leq 19 - 7$$

$$-9 < 3x \leq 12$$

$$\text{① S.B.N. } \{x \mid -3 < x \leq 4\}$$

$$\frac{-9}{3} < x \leq \frac{12}{3}$$

$$\text{② Graph } \leftarrow \left(-3 \right] 4 \rightarrow$$

$$-3 < x \leq 4$$

$$\text{③ I.N. } (-3, 4]$$

$$5 < -2x - 3 \leq 9$$

$$\text{Add } 3 \rightarrow -4 > x \geq -6$$

$$8 \boxed{<} -2x \boxed{\leq} 12$$

$$\text{I.N. } [-6, 4)$$

$$\boxed{-6 \leq x < -4}$$

$$\text{① S.B.N. } \{x \mid -6 \leq x < -4\}$$

$$\frac{8}{-2} > \frac{-2}{-2}x \geq \frac{12}{-2}$$

$$\text{② Graph } \leftarrow [-6, -4) \rightarrow$$

$2x - 3y = 9$, write in $y = mx + b$ form.

$$-3y = -2x + 9$$

$$y = \frac{-2}{-3}x + \frac{9}{-3} \Rightarrow y = \frac{2}{3}x - 3$$

Evaluate $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ for $a=1$,
 $b=-2$,
 $c=-24$

$$= \frac{-(-2) \pm \sqrt{(-2)^2 - 4(1)(-24)}}{2(1)} = \frac{2 \pm \sqrt{4 + 96}}{2}$$

$$= \frac{2 \pm \sqrt{100}}{2} = \frac{2 \pm 10}{2} = \frac{12}{2} = \boxed{6}$$

Evaluate: $\frac{x-5}{x^2-4}$ for $x=0, 5, -2$.

$$\frac{0-5}{0^2-4} = \frac{-5}{-4} = \boxed{\frac{5}{4}}$$

$$\frac{5-5}{5^2-4} = \frac{0}{25-4} = \frac{0}{21} = \boxed{0}$$

$$\frac{-2-5}{(-2)^2-4} = \frac{-7}{4-4} = \frac{-7}{0}$$

\emptyset

Name the Prop.

$$\textcircled{1} 4(x-2) = 4 \cdot x - 4 \cdot 2$$

Distributive

$$\textcircled{2} 5(7x) = (5 \cdot 7)x$$

Associative

Associative
Inverse
Identity

$$\textcircled{3} -8x + 8x = 0$$

Inverse

$$\textcircled{4} \frac{2}{3} \left(\frac{3}{2}x \right) = \left(\frac{2}{3} \cdot \frac{3}{2} \right)x = 1 \cdot x = x$$

Whole numbers $0, 1, 2, 3, 4, \dots$

Integers $\dots, -5, -4, -3, -2, -1, 0, 1, 2, 3, \dots$

Consecutive integers

$23, 24, 25, 26, \dots$

$99, 100, 101, 102, 103, \dots$

$-33, -32, -31, -30, -29, \dots$

$x, x+1, x+2, x+3, \dots$

Find two consecutive integers such that their sum is 51.

First: x

Second: $x+1$

$$\text{First} + \text{Second} = 51$$

$$x + x + 1 = 51$$

$$2x + 1 = 51$$

$$2x = 50$$

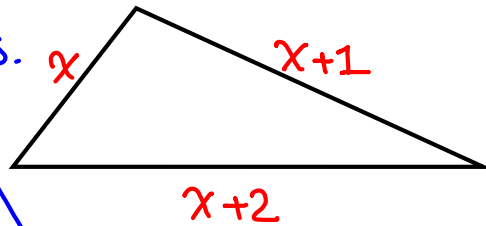
$$x = 25$$

$25 \text{ \& } 26$

Perimeter of a triangle is 54 ft.

Three sides are three consecutive integers.

Find all three sides.



$$P = 54$$

$$a + b + c = 54$$

$$x + x+2 + x+1 = 54$$

$$3x + 3 = 54$$

$$3x = 51$$

$$x = 17$$

17 ft, 18 ft, and 19 ft.

A rectangular garden has a perimeter of 42m.

Length and width are two cons. integers.

Find its dimensions and find its Area.

$$\begin{array}{l} P = 2L + 2W \\ A = LW \end{array}$$

$$W = x$$

$$L = x+1$$

10m by 11m

$$A = 10(11) = 110m^2$$

$$P = 42$$

$$2L + 2W = 42$$

$$2(x+1) + 2(x) = 42$$

$$2x + 2 + 2x = 42$$

$$4x + 2 = 42$$

$$4x = 40$$

$$x = 10$$

Consecutive even integers

6, 8, 10, 12, ----

90, 92, 94, ----

-32, -30, -28, -26, ----

$x, x+2, x+4, x+6, \dots$; x must be even

Find two cons. even integers with the

Sum of 82

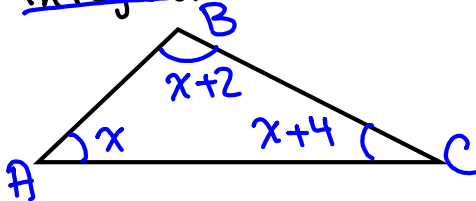
$\hookrightarrow x \text{ \& } x+2$

$$x + x + 2 = 82$$

$$2x = 80 \rightarrow x = 40$$

40 \& 42

the measure of all three interior angles in triangle ABC are three cons. even integers. Find all three angles.



Fact: $\underbrace{m\angle A} + \underbrace{m\angle B} + \underbrace{m\angle C} = 180^\circ$

$$x + x + 2 + x + 4 = 180^\circ$$

$$3x + 6 = 180$$

$$3x = 174$$

$$x = 58$$

58°, 60°, and 62°

Find two consecutive even integers such that the difference of 3 times the smaller one and the larger one is 42.

$$3 \cdot \text{Smaller} - \text{larger} = 42$$

Smaller $\rightarrow x$

Larger $\rightarrow x+2$

$$3 \cdot x - (x+2) = 42$$

$$3x - x - 2 = 42$$

$$2x = 44$$

$$x = 22$$

$$22 \text{ \& } 24$$

check

$$3 \cdot 22 - 24 = 66 - 24 = 42$$

Find three consecutive even integers such that the sum of the first one and 3 times the second one is equal to 98 more than the third one.

First $\rightarrow x$

Second $\rightarrow x+2$

Third $\rightarrow x+4$

$$\boxed{\text{First}} + 3 \boxed{\text{Second}} = \boxed{\text{Third}} + 98$$

$$x + 3(x+2) = x+4 + 98$$

$$x + 3x + 6 = x + 102 \rightarrow 3x = 96$$

$$4x + 6 = x + 102$$

$$x = 32$$

$$4x - x = 102 - 6$$

$$32, 34, \text{ and } 36$$

Consecutive odd integers:

1, 3, 5, 7, ---

105, 107, 109, 111, ---

-51, -49, -47, -45, -43, ---

$x, x+2, x+4, x+6, \dots$; x must be odd.

Find two consecutive odd integers with the total of 36.

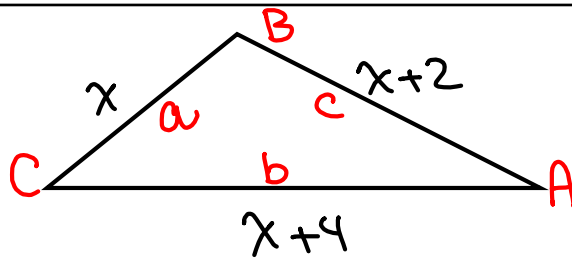
$\rightarrow x \text{ \& } x+2$

$$x + x+2 = 36$$

$$2x = 34 \rightarrow x = 17$$

17 \& 19

The perimeter of a rose garden in a triangle shape is 75 ft. Sides are 3 Cons. odd integers. Draw \& label them Find all three sides.



$$P = 75$$

$$a + b + c = 75$$

$$x + x + 4 + x + 2 = 75$$

23 ft, 25 ft, and 27 ft

$$3x + 6 = 75$$

$$3x = 69$$

$$x = 23$$

I paid \$152.25 for a microwave.

this included 8.75% sales tax.

what was the price of the microwave?

Price of Microwave $\rightarrow x$

Amount of Sales tax $\rightarrow 8.75\%$ of x

Total cost $\rightarrow 152.25$

$$x + 8.75\% \text{ of } x = 152.25$$

$$x + .0875x = 152.25$$

$$1.0875x = 152.25$$

$$\rightarrow x = \frac{152.25}{1.0875}$$

$$x = 140$$

\$140

Solve for π : $V = \frac{4\pi r^3}{3}$

Hint: Clear fraction

LCD=3

$$3V = 4\pi r^3$$

Divide by
 $4r^3$

$$\frac{3V}{4r^3} = \frac{\cancel{4\pi r^3}}{\cancel{4r^3}}$$

$$\boxed{\frac{3V}{4r^3} = \pi}$$

Solve for r : $A = \textcircled{P} + Prt$

$$A - P = \textcircled{P}rt$$

Exam I:

Tuesday

Due Tomorrow

SG 5

Also work on

SG 6 & SG 7

WP 5 & WP 6

$$\frac{A - P}{Pt} = \frac{\cancel{P}rt}{\cancel{Pt}}$$

$$\boxed{\frac{A - P}{Pt} = r}$$

Expect a Quiz tomorrow.